

Sejam u e v funções variáveis de z e n constante.

Derivadas

- $y = u^n \Rightarrow y' = nu^{n-1}u'$
- $y = uv \Rightarrow y' = u'v + v'u$
- $y = \frac{u}{v} \Rightarrow y' = \frac{u'v - v'u}{v^2}$
- $y = a^u \Rightarrow y' = a^u(\ln a)u', (a > 0, a \neq 1)$
- $y = e^u \Rightarrow y' = e^u u'$
- $y = \log_a u \Rightarrow y' = \frac{u'}{u} \log_a e$
- $y = \ln u \Rightarrow y' = \frac{1}{u} u'$
- $y = u^v \Rightarrow y' = vu^{v-1}u' + u^v(\ln u)v'$
- $y = \sin u \Rightarrow y' = u' \cos u$
- $y = \cos u \Rightarrow y' = -u' \sin u$
- $y = \tan u \Rightarrow y' = u' \sec^2 u$
- $y = \cot u \Rightarrow y' = -u' \csc^2 u$
- $y = \sec u \Rightarrow y' = u' \sec u \cdot \tan u$
- $y = \csc u \Rightarrow y' = -u' \csc u \cdot \cot u$
- $y = \arcsin u \Rightarrow y' = \frac{u'}{\sqrt{1-u^2}}$
- $y = \arccos u \Rightarrow y' = \frac{-u'}{\sqrt{1-u^2}}$
- $y = \arctan u \Rightarrow y' = \frac{u'}{\sqrt{1+u^2}}$
- $y = \text{arccot } u \Rightarrow y' = \frac{-u'}{\sqrt{1+u^2}}$
- $y = \text{arcsec } u, |u| \geq 1 \Rightarrow y' = \frac{u'}{|u|\sqrt{u^2-1}}, |u| > 1$
- $y = \text{arccsc } u, |u| \geq 1 \Rightarrow y' = \frac{-u'}{|u|\sqrt{u^2-1}}, |u| > 1$

Identidade trigonométricas

- $\sin^2 x + \cos^2 x = 1$
- $1 + \tan^2 x = \sec^2 x$
- $1 + \cot^2 x = \csc^2 x$
- $\sin^2 x = \frac{1 - \cos 2x}{2}$
- $\cos^2 x = \frac{1 + \cos 2x}{2}$
- $\sin 2x = 2 \sin x \cdot \cos x$
- $2 \sin x \cdot \cos y = \sin(x - y) + \sin(x + y)$
- $2 \sin x \cdot \sin y = \cos(x - y) - \cos(x + y)$
- $\cos x \cdot \cos y = \cos(x - y) + \cos(x + y)$
- $1 \pm \sin x = 1 \pm \cos\left(\frac{\pi}{2} - x\right)$

Integrais

- $\int du = u + c$
- $\int u^n du = \frac{u^{n+1}}{n+1} + c, n \neq -1$
- $\int \frac{du}{u} = \ln |u| + c$
- $\int a^u du = \frac{a^u}{\ln a} + c, a > 0, a \neq 1$
- $\int e^u du = e^u + c$
- $\int \sin u \cdot du = -\cos u + c$
- $\int \cos u \cdot du = \sin u + c$
- $\int \tan u \cdot du = \ln |\sec u| + c$
- $\int \cot u \cdot du = \ln |\sin u| + c$
- $\int \sec u \cdot du = \ln |\sec u + \tan u| + c$
- $\int \csc u \cdot du = \ln |\csc u - \cot u| + c$
- $\int \sec u \cdot \tan u \cdot du = \sec u + c$
- $\int \csc u \cdot \cot u \cdot du = -\csc u + c$
- $\int \sec^2 u \cdot du = \tan u + c$
- $\int \csc^2 u \cdot du = -\cot u + c$
- $\int \frac{du}{u^2+a^2} = \frac{1}{a} \arctan \frac{u}{a} + c$
- $\int \frac{du}{u^2-a^2} = \frac{1}{2a} \ln \left| \frac{u-a}{u+a} \right| + c, u^2 > a^2$
- $\int \frac{du}{\sqrt{u^2+a^2}} = \ln |u + \sqrt{u^2+a^2}| + c$
- $\int \frac{du}{\sqrt{u^2-a^2}} = \arcsin \frac{u}{a} + c, u^2 < a^2$
- $\int \frac{du}{\sqrt{a^2-u^2}} = \arcsin \frac{u}{a} + c, u^2 < a^2$
- $\int \frac{du}{u\sqrt{a^2-u^2}} = \frac{1}{a} \text{arcsec} \left| \frac{u}{a} \right| + c$

Fórmulas de recorrência

- $\int \sin^n au \cdot du = -\frac{\sin^{n-1} au \cdot \cos au}{an} + \left(\frac{n-1}{n}\right) \cdot \int \sin^{n-2} au \cdot du$
- $\int \cos^n au \cdot du = \frac{\sin au \cos^{n-1} au}{an} + \frac{n-1}{n} \cdot \int \cos^{n-2} au \cdot du$
- $\int \tan^n au \cdot du = \frac{\tan^{n-1} au}{a(n-1)} - \int \tan^{n-2} au \cdot du$
- $\int \cot^n au \cdot du = -\frac{\cot^{n-1} au}{a(n-1)} - \int \cot^{n-2} au \cdot du$
- $\int \sec^n au \cdot du = \frac{\sec^{n-2} au \tan au}{a(n-1)} + \frac{n-2}{n-1} \int \sec^{n-2} au \cdot du$
- $\int \csc^n au \cdot du = -\frac{\csc^{n-2} au \cot au}{a(n-1)} + \frac{n-2}{n-1} \int \csc^{n-2} au \cdot du$